Guiding principles of light in frustrated chiral birefringent systems

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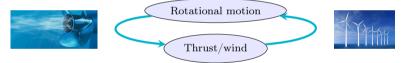


Outline

- Introduction
- 2 Light propagation in anisotropic media
- 3 Role of chirality in the non-linear reponse of a confined cholesteric
- 4 Interaction between light and topological solitons
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Chirality in everyday life

- Chiral object: distinguishable from its mirror image.
- A common example: propeller.



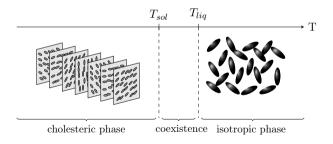
• Without chirality, this conversion is not possible.

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- \bullet Nematic phase + chiral molecules: cholesteric phase.

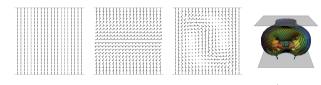
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Frustration: confining cholesterics between two plates

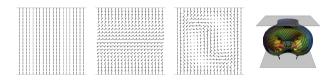
• Surface constraint: molecules must be normal to the confining surface



increasing sample thickness

Frustration: confining cholesterics between two plates

• Surface constraint: molecules must be normal to the confining surface



increasing sample thickness

• Arbitrary shapes can be written with thread-like structures!





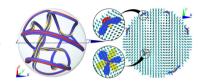




P. J. Ackerman et al., Scientific Reports 2 (2012)

Frustration: confining cholesterics inside droplets

Topological zoo of free standing knots



Lasing in a cholesteric droplet: an omnidirectional microscopic coherent light source



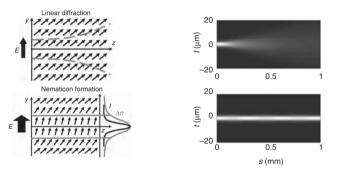


D. Seč, S. Čopar and S. Žumer, $Nature\ communications\ {\bf 5}\ (2014)$

M. Humar, Liquid Crystals 43 (2016)

Problematics

Non-linear optical response of liquid crystal systems:



Increasing beam power

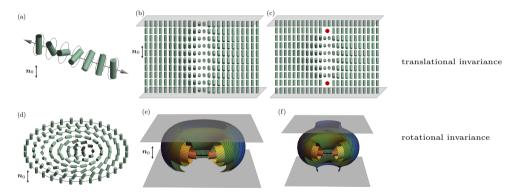
G. Assanto. Nematicons. John Wiley & Sons, 2013

Problematic 1

Role of chirality in the non-linear optical response of a frustrated cholesteric?

Problematics

Two classes of soft chiral topological solitons in frustrated cholesterics



Problematic 2

Localized and robust chiral birefringent structures ⇒ interesting interaction with light?

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• Recent advances in LC-based light application: tunable microresonators, micro-optical elements, diffraction gratings...

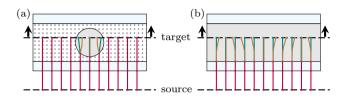
- Recent advances in LC-based light application: tunable microresonators, micro-optical elements, diffraction gratings...
- Simulation tools for light propagation:
 - * Jones method (fast but inacurate, easy to code)
 - * Finite Difference Time Domain (acurate but slow, open-source, complex to use)
 - * Other methods (in-house implementation)

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Need for advanced light propagation code, if possible open-source

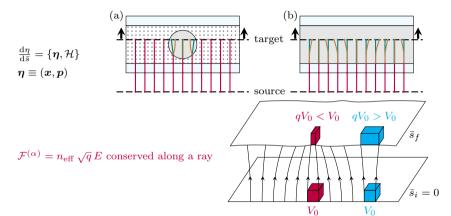
First approach: Hamiltonian ray-tracing and energy transport





G. Poy and S. Žumer, Soft Matter 15 (2019)

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Advantage: intuitive physical interpretation

G. Poy and S. Žumer, Soft Matter 15 (2019)

Second approach: physics-based splitting of the wave equation

• Wave-equation in anisotropic media: $\left[\partial_k \partial_k \delta_{ij} - \partial_i \partial_j + k_0^2 \epsilon_{ij}\right] E_j = 0$

G. Poy and S. Žumer, Optics Express 28 (2020)

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- Wave-equation in anisotropic media: $\left[\partial_k \partial_k \delta_{ij} \partial_i \partial_j + k_0^2 \epsilon_{ij}\right] E_j = 0$
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$$i\partial_z oldsymbol{E}_\perp = - oldsymbol{\mathcal{P}} oldsymbol{E}_\perp$$

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• What's inside \mathcal{P} ?



Phase op. $\mathbf{K} \sim k_0^2 \boldsymbol{\epsilon}$



Walkoff op. $\boldsymbol{W} \sim (\boldsymbol{\epsilon} \, \boldsymbol{u}_z) \otimes \boldsymbol{\nabla}_{\perp}$



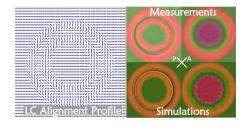
Diffraction op. $\boldsymbol{D} \sim \boldsymbol{\Delta}_{\perp}$

Advantage: fast and accurate simulations

G. Poy and S. Žumer, Optics Express 28 (2020)

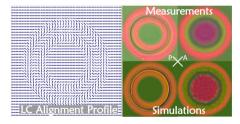
Nemaktis: an open-source package for polarised microscopy

- The open-source package includes:
 - Low-level simulation backends (C++, python)
 - An easy-to-use high-level interface (python)
 - A graphical interface for micrographs simulation



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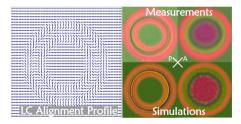


• Where to find it: search **Nemaktis** on **github.com** or **google**.

B. Berteloot et al., Soft Matter 16 (2020)

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- Where to find it: search **Nemaktis** on **github.com** or **google**.
- Closed-source BPM code for advanced uses: wide-angle beam deflection, non-linear optics, etc.
 - B. Berteloot et al., Soft Matter 16 (2020)

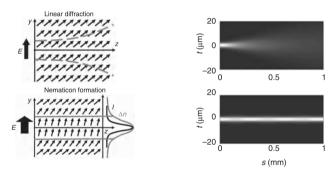
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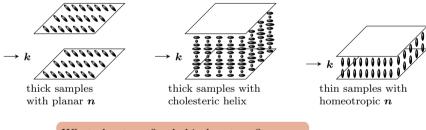
Spatial light solitons in liquid crystals: nematicons



G. Assanto. Nematicons. John Wiley & Sons, 2013

Increasing beam power

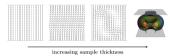
Studied systems in the past 20 years:



What about confined chiral systems?

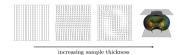
What makes frustrated cholesteric (FCLC) an interesting system:

ullet Metastability for carefully chosen values of d/P

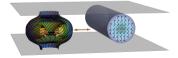


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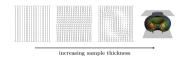


 \bullet Rich possibilities of interaction between light beams and topological solitons.

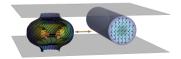


What makes frustrated cholesteric (FCLC) an interesting system:

• Metastability for carefully chosen values of d/P



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Problematic

Can we generate light solitons in frustrated cholesteric?

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Orientational elasticity and non-linear interactions

Free energy of the liquid crystal phase:

$$F[\boldsymbol{n}, \boldsymbol{E}] = \int_{V} dV \left[f_{F}(\boldsymbol{n}, \nabla \boldsymbol{n}) - \frac{\epsilon_{0} \epsilon_{a} |\boldsymbol{n} \cdot \boldsymbol{E}|^{2}}{4} \right]$$

Orientational elasticity and non-linear interactions

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Non-linear iterative scheme:

- E_{k+1} : BPM solution with $\epsilon = \epsilon_{\perp} \mathbf{I} + \epsilon_a \mathbf{n}_k \otimes \mathbf{n}_k$
- ullet $oldsymbol{n}_{k+1} = oldsymbol{n}_k + \mu rac{\delta F}{\delta oldsymbol{n}} \left[oldsymbol{n}_k, oldsymbol{E}_{k+1}
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Orientational elasticity and non-linear interactions

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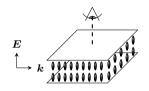
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Typical running time for a mesh of 3×10^6 points: 4 s / step (Full resolution of Maxwell equations for the same mesh: $\sim 1 \text{ h}$)

Top-view observations



Top view of the thickness-averaged laser intensity (simulation):

Linear optical regime

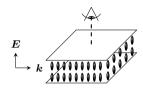
Non-linear optical regime

Top view of the scattered laser light (experiments):

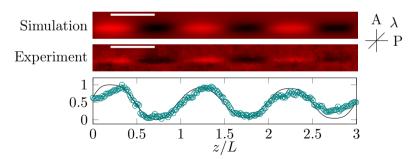
Linear optical regime

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Top-view observations

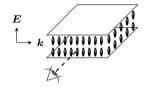


Top view polarised optical micrograph:

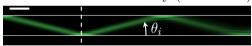


G. Poy

Why is there a periodic molecular reorientation?



Side slice of beam intensity (simulation):



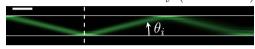
Side slice of 3PF signal (experiment):



G. Poy

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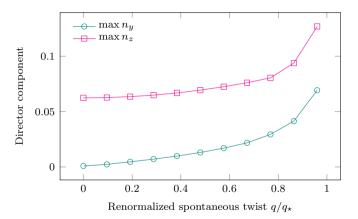
Side slice of director field



Mid-sample slice of director field

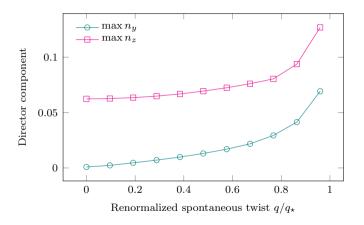


Chirality-enhanced non-linear optical response



G. Poy et al., Physical Review Letters 125 (2020)

Chirality-enhanced non-linear optical response



 \Rightarrow Potential for low-power non-linear optical photonics devices (e.g. active lenses)

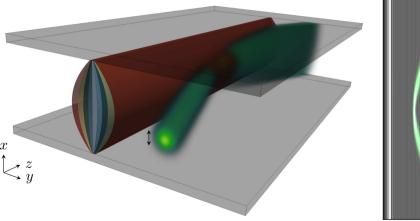
G. Poy et al., Physical Review Letters 125 (2020)

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Transmission and/or reflection with line-like structure

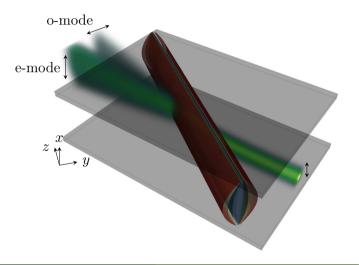
Reflection of incident extraordinary beam ($\theta_i = 70^{\circ}$):





Transmission and/or reflection with line-like structure

Transmission of incident extraordinary beam ($\theta_i = 55^{\circ}$):





From an exact eigenmode decomposition of Maxwell equations:

$$n^{(\alpha,m)}\sin\theta^{(\alpha,m)} = n_i\sin\theta_i$$

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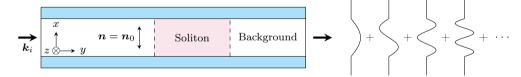
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 \bullet Usual Snell law: n is the refractive index of an isotropic medium

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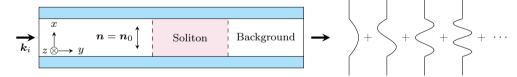
- ullet Usual Snell law: n is the refractive index of an isotropic medium
- In our system, $n^{(\alpha,m)} = \text{effective index of eigenmode } \{\alpha, m\}$ far from the soliton
 - $\star \alpha = e, o$: polarisation state
 - $\star m = 1, 2, \ldots$ mode index



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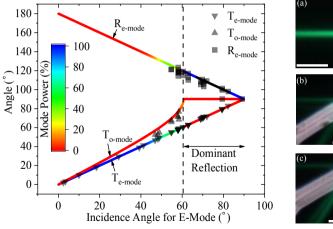
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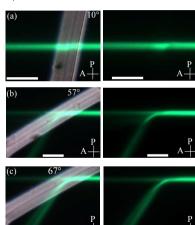


 $\theta^{(\alpha,m)}$ does not depends on the choice of topological soliton! (but Fresnel coefficients do)

Comparison with experiments

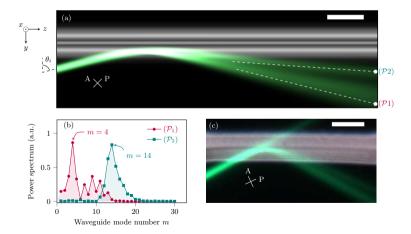
Small mode index approximation in thick samples: $n^{(\alpha,m)} \approx n_{\alpha} \sqrt{1 - (m/m_0)^2} \approx n_{\alpha}$





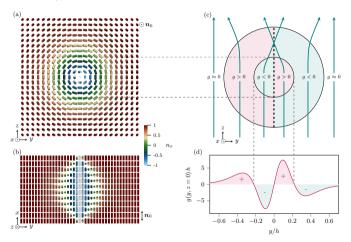
Comparison with experiments

Splitting of eigenmode packets (strongly depends on x-profile): $n^{(\alpha,m_1)} \neq n^{(\alpha,m_2)}$

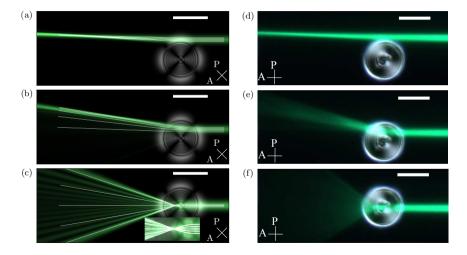


Interaction with point-like topological solitons

Simplification with 2D rays: $dp_y/dz \approx -(\epsilon_a/2n_0)g$, where $g \equiv \partial n_z^2/\partial y$



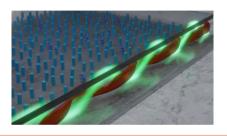
Light deflection and lensing with pinned torons

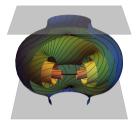


A. Hess et al., Physical Review X 10 (2020)

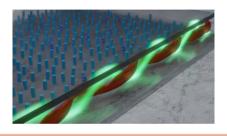
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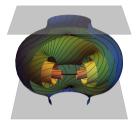
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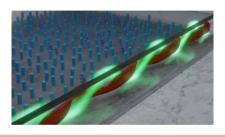
Chirality and soft topological solitons unlocks new possiblities to control the flow of light at the microscopic level

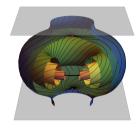




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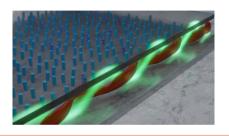
• Chirality-enhanced optical response: towards enriched opto-mechanical interactions

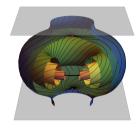




Chirality and soft topological solitons unlocks new possiblities to control the flow of light at the microscopic level

- Chirality-enhanced optical response: towards enriched opto-mechanical interactions
- Matter transforming light, light transforming matter: what happens when we combine everything?





Chirality and soft topological solitons unlocks new possiblities to control the flow of light at the microscopic level

- Chirality-enhanced optical response: towards enriched opto-mechanical interactions
- Matter transforming light, light transforming matter: what happens when we combine everything?

Next step: establishment of a general chirality-enhanced topological optomechanics framework.